



Information & Communication Security (SS 2022)

Cryptography I

Prof. Dr. Kai Rannenberg

Chair of Mobile Business & Multilateral Security Goethe University Frankfurt a. M.





- Introduction
- Symmetric Key Cryptography
 - General Process
 - Substitution Ciphers
 - Caesar Cipher
 - Vigenére Cipher
 - One Time Pad
 - AES
 - Advantages and Problems
- Public Key Cryptography
- Outlook and Post-Quantum Cryptography

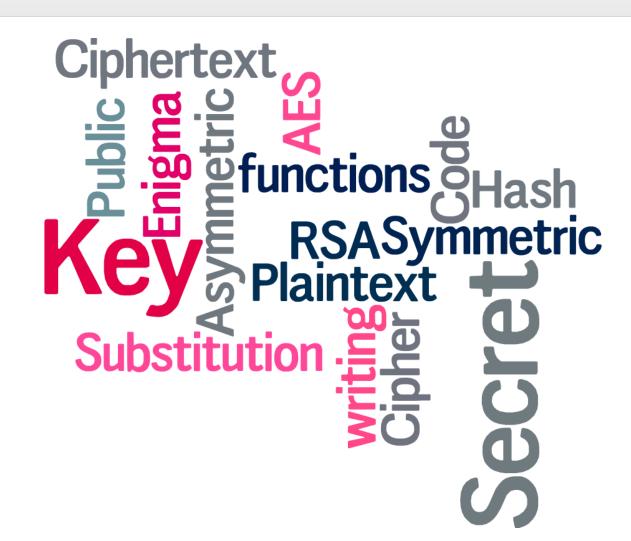




- Introduction
- Symmetric Key Cryptography
 - General Process
 - Substitution Ciphers
 - Caesar Cipher
 - Vigenére Cipher
 - One Time Pad
 - AES
 - Advantages and Problems
- Public Key Cryptography
- Outlook and Post-Quantum Cryptography



Cryptography





Cryptosystem

A Cryptosystem is a 5-tuple (**P,K,C,E,D**)

A set **P** of plaintexts

A set **K** of keys

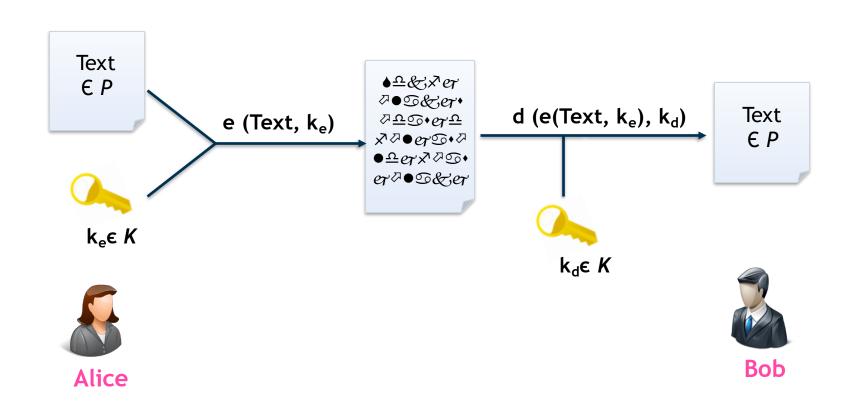
A set *C* of ciphertexts

A set *E* of enciphering functions, with *E*: *P* x *K* -> *C*

A set D of deciphering functions, with *D*: *C x K* -> *P*



Example





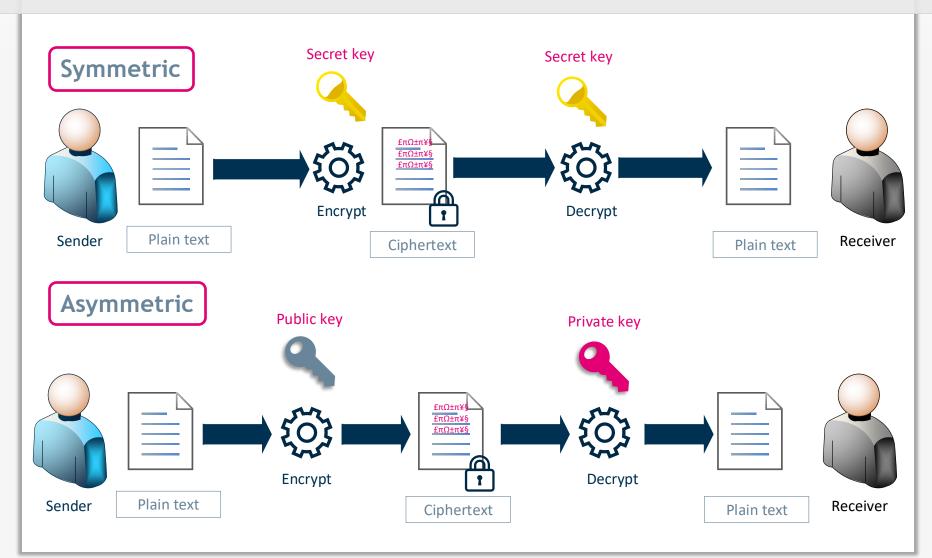
Cryptographic Systems (I)

- Intention
 - Confidentiality (secrecy of messages): encryption systems
 - Integrity (protection from undetected manipulation) and accountability:
 authentication systems and digital signature systems
- Key distribution
 - Symmetric: Both partners have the same key.
 - Asymmetric:
 Different (but related) keys for encryption and decryption

In practice mostly hybrid systems



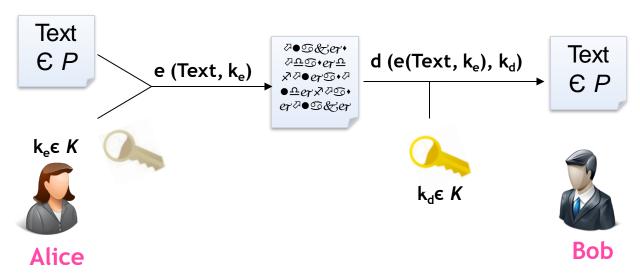
Cryptographic Systems (II)





Kerckhoffs' Principle

- The principle (first stated in 1883):
 - The secret lies within the key and not within the algorithm;
 - Thus "Security through obscurity" is not a sustainable solution.
- In our small example:
 - Separation of algorithm $m{e}$ and key $m{k_e}$





Cryptography - Important Concepts

- Shannon's perfect secrecy
 - All plaintexts have the same probability for a given ciphertext.
- One-Time Pad Shannon / Vernam
 - Theoretically completely unbreakable, but highly impractical
- Shannon's concepts: Confusion and Diffusion
 - Relation between M, C, and K should be as complex as possible (M = message, C = cipher, K = key)
 - Every ciphertext character should depend on as many plaintext characters and as many characters of the encryption key as possible.
 - "Avalanche effect" (small modification, big impact)
- Trapdoor function (one-way function)
 - Fast in one direction, not in the opposite direction (without secret information)
 - Knowing the secret allows the function to work in the opposite direction (access to the trapdoor).





- In a *ciphertext only* attack, the adversary has only the ciphertext. Her goal is to find the corresponding plaintext. If possible, she may try to find the key, too.
- In a known plaintext attack, the adversary has the plaintext and the ciphertext that was enciphered. Her goal is to find the key that was used.
- In a *chosen plaintext* attack, the adversary may ask that specific plaintexts be enciphered. She is given the corresponding ciphertexts. Her goal is to find the key that was used.





- Introduction
- Symmetric Key Cryptography
 - General process
 - Substitution ciphers
 - Caesar cipher
 - Vigenére cipher
 - One time pad
 - AES
 - Advantages and Problems
- Public key cryptography



Symmetric Key Cryptography

Symmetric Encryption Systems
Applications & Examples

- Classical cryptosystems are usually based on symmetric encryption systems.
- Typical applications
 - confidential storage of user data
 - transfer of data between 2 users who negotiate a key via a secure channel
- Examples
 - Vernam-Code (one-time pad, Gilbert Vernam)
 - key length = length of the plaintext (information theoretically secure)
 - DES: Data Encryption Standard
 - key length 56 bit, so 2⁵⁶ different keys
 - AES: Advanced Encryption Standard (Rijndael, [NIST])
 - 3 alternatives for key length: 128, 192 und 256 bit

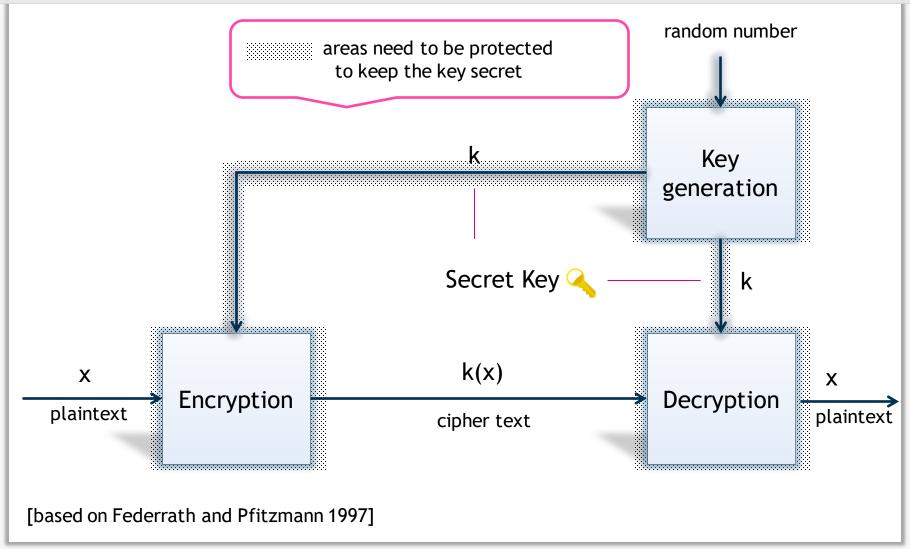




- Introduction
- Symmetric Key Cryptography
 - General process
 - Substitution ciphers
 - Caesar cipher
 - Vigenére cipher
 - One time pad
 - AES
 - Advantages and Problems
- Public key cryptography

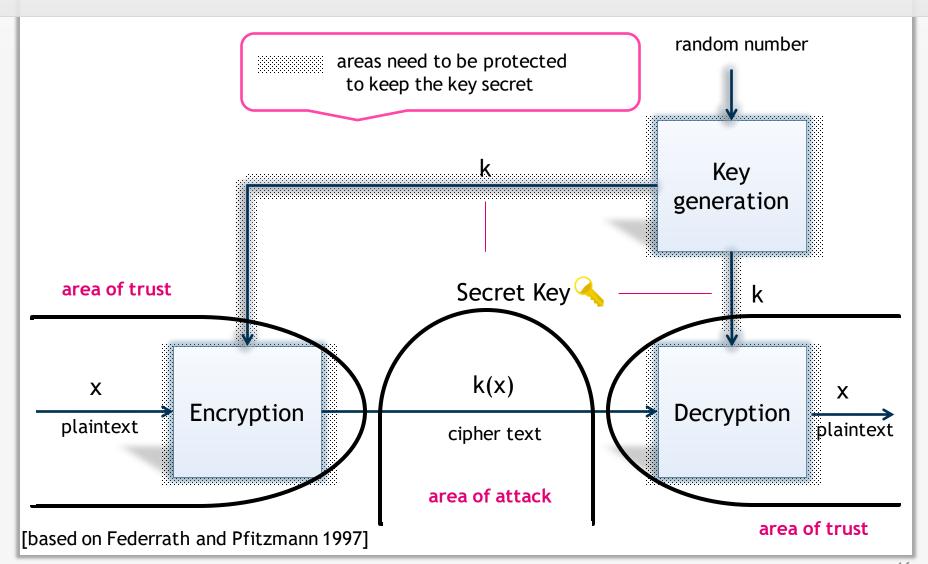


Symmetric Key Cryptography General Process





Symmetric Key Cryptography General Process





Symmetric Key Cryptography General Process

- Keys have to be kept secret (secret key crypto system).
- It must not be possible to infer on the plaintext or the keys used from the encrypted text (ideally encrypted text is not distinguishable from a numerical random sequence).
- Each key shall be equally probable.
- In principle each system with limited key length is breakable by testing all possible keys.
- Publication of encrypting and decrypting functions (algorithms) is considered as good style and is trust-building.
- Security of cryptosystems should base on the strength of chosen key lengths.





- Introduction
- Symmetric Key Cryptography
 - General process
 - Substitution ciphers
 - Caesar cipher
 - Vigenére cipher
 - One time pad
 - AES
 - Advantages and Problems
- Public key cryptography



Caesar Cipher

Α	В	C	D	E	F	G	Н		J	K	L	M
0	1	2	3	4	5	6	7	8	9	10	11	12
N	0	Р	Q	R	S	Т	U	V	W	Χ	Υ	Z

- We assign a number for every character.
- This enables us to calculate with letters as if they were numbers.

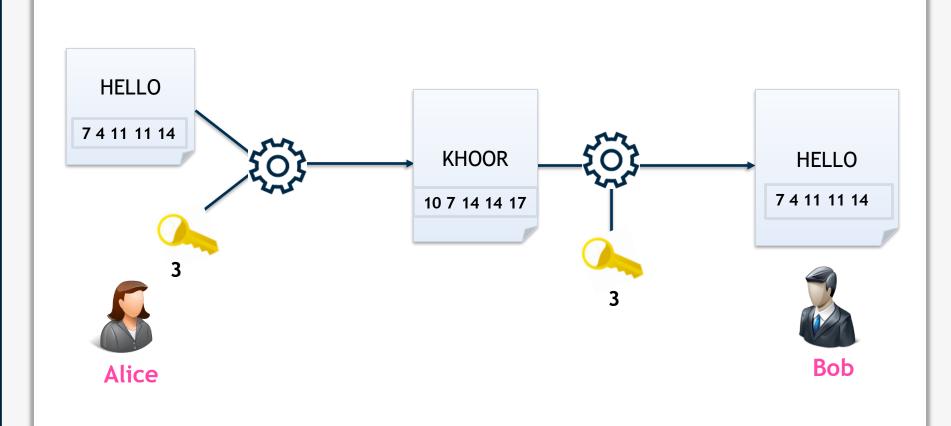


Caesar Cipher

- For k ε {0...25} we have:
 - An encryption function:
 - e: x -> (x+k) mod 26
 - A decryption function:
 - d: x -> (x-k) mod 26
 - In this case k_e = k_d



Example





Some Attacks

- In case of a known plaintext attack it is trivial to get the key used.
- There are only 26 possible keys. This cipher is therefore vulnerable to a brute force attack.
- This cipher is also vulnerable to a statistical ciphertext-only attack.



Assessment of Caesar Cipher

- Of course this is a very simple form of encryption.
- The encryption and decryption algorithms are very easy and fast to compute.
- It uses a very limited key space (n=26).
- Therefore, the encryption is very easy and fast to compromise.



Can We Make it More Secure?

- Use a permutation of the alphabet as the key.
- Example:

"HELLO" -> "ITSSG"





- Use of permutations increases the key space.
- Therefore, a brute force attack becomes more difficult.
- The encryption and decryption are not much harder to compute.
 - Table lookup
- Still vulnerable to a statistical ciphertextonly attack.



Statistical Ciphertext-only Attack

- Use statistical frequency of occurrence of single characters to figure out the key.
- Language dependent
- Frequencies of character pairs (bigrams) may also be used

E	11.1607%	M	3.0129%
A	8.4966%	Н	3.0034%
R	7.5809%	G	2.4705%
I	7.5448%	В	2.0720%
O	7.1635%	F	1.8121%
\mathbf{T}	6.9509%	Υ	1.7779%
N	6.6544%	W	1.2899%
S	5.7351%	K	1.1016%
L	5.4893%	٧	1.0074%
C	4.5388%	X	0.2902%
\mathbf{U}	3.6308%	Z	0.2722%
D	3.3844%	J	0.1965%
P	3.1671% (English)	Q	0.1962%
	(=11511311)		

[www.oxforddictionaries.com/words/what-is-the-frequency-of-the-letters-of-the-alphabet-in-english]





- Introduction
- Symmetric Key-Cryptography
 - General process
 - Substitution ciphers
 - Caesar cipher
 - Vigenére cipher
 - One time pad
 - AES
 - Advantages and Problems
- Public key cryptography



Vigenére Cipher

- The Vigenére cipher chooses a sequence of keys, represented by a string.
- The key letters are applied to successive plaintext characters.
- When the end of the key is reached, the key starts over.
- The length of the key is called the period of the cipher.



Vigenére Tableau

Example

- Let the message be "THE BOY HAS THE BAG"
- and let the KEY be "VIG"

```
PT= T H E B O Y H A S T H E B A G

K= V I G V I G V I G V I G V I G

CT= O P K W W E C I Y O P K W I M
```



Assessment Vigenére Cipher

- For many years, the Vigenére cipher was considered unbreakable.
- Then a Prussian cavalry officer named Kasiski noticed that repetitions occur when characters of the key appear over the same characters in the plaintext.
- The number of characters between successive repetitions is a multiple of the period (key length).
- Given this information and a short period the Vigenére cipher is quite easily breakable.
- Example: The Caesar cipher is a Vigenére cipher with a period of 1.



Example Vigenére Cipher

 Let the message be "THE BOY HAS THE BAG "and let the key be "VIG ":

Plaintext:

T H E B O Y H A S T H E B A G

Key:

• Ciphertext: OPKWWECIYOPKWI



Example

A B C D E F G H I J K L M N O P Q R S T U V W X Y Z

Example

- Let the message be "HELLO"
- and let the KEY be "SEC"
- a=ZINLO
- b=ZINDS
- c=ZENNO





- Introduction
- Symmetric Key Cryptography
 - General process
 - Substitution ciphers
 - Caesar cipher
 - Vigenére cipher
 - One time pad
 - AES
 - Advantages and Problems
- Public key cryptography



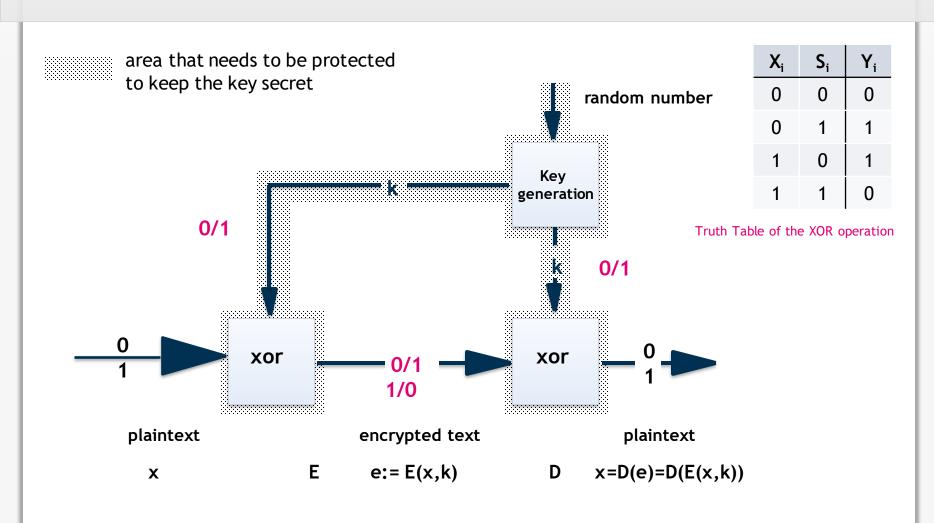
One Time Pad

- Invented by Gilbert Vernam
- The one-time pad is basically a Vigenére cipher.
- The length of the key is as long as the length of the plaintext.
- Therefore, there are no periodic reoccurrences.
- The key is randomly chosen and only used once.
- Every key has the same probability.



[based on Federrath and Pfitzmann 1997]

Example One Time Pad





Example

PT=	0	1	1	0
k=	1	0	1	1

X _i	S_{i}	Yi
0	0	0
0	1	1
1	0	1
1	1	0

Truth Table of the XOR operation

a=	1	1	1	1
b=	1	0	1	1
C=	1	1	0	1



Assessment One Time Pad

- The one time pad is unbreakable by ciphertext only attacks.
 - Example: Let the ciphertext be "FGHA".
 - Since we know the key length is at least 4 and the probability of every possible key is equal, the plaintext can be any 4-letter word possible.
- In a known plaintext attack we can deduct the key.
 - Then we know which key was used to encrypt the message we already know.
 - But the next message is encrypted with a different key, because every key is only used once.
- The same applies to a chosen plaintext attack.
- The one-time pad is information theoretically secure and provably impossible to break.





- Introduction
- Symmetric Key Cryptography
 - General process
 - Substitution ciphers
 - Caesar cipher
 - Vigenére cipher
 - One time pad
 - AES
 - Advantages and Problems
- Public key cryptography

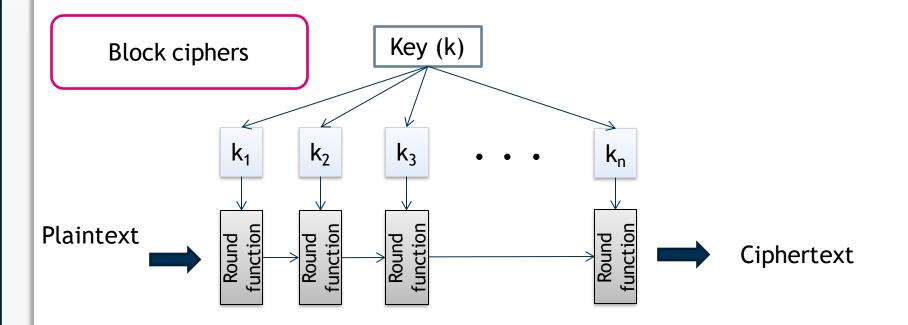


Advanced Encryption Standard (AES) - History

- The Data Encryption Standard (DES) was designed to encipher sensitive but not classified data.
- The standard has been issued in 1977.
- In 1998, a design for a computer system and software that could break any DES-enciphered message within a few days was published.
- By 1999, it was clear that the DES no longer provided the same level of security it had 10 years earlier, and the search was on for a new, stronger cipher.
- AES Rijndael was a winner of U.S. National Institute of Standards and Technology bid for advanced encryptions.
- AES has been approved for Secret or even Top Secret information by the NSA.



AES - Functionality



- Variable number of rounds (10, 12, 14)
- Depending on key size (128-bit, 192-bit, 256-bit).

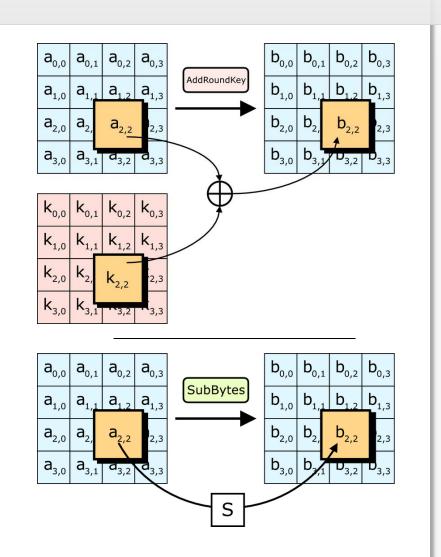
[Bi2005]



Encryption Round (1)

AES

- AddRoundKey
 - XOR (mix bits of) current state a and round key
 - Round key k derived using key schedule
- SubBytes
 - Substitution using a lookup table (S-Box)

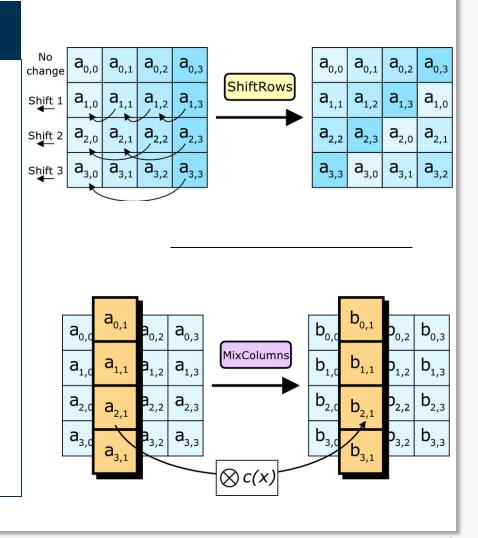




Encryption Round (2)

AES

- ShiftRows
 - Shift each row by row index
- MixColumns
 - 4 key bytes combined into each column using polynomial multiplication modulo 2⁸ [in GF(2⁸)]
 - GF = Galois field = finite field







- Introduction
- Symmetric Key Cryptography
 - General process
 - Substitution ciphers
 - Caesar cipher
 - Vigenére cipher
 - One time pad
 - AES
 - Advantages and Problems
- Public key cryptography



Symmetric Encryption

Advantage: Algorithms are very fast

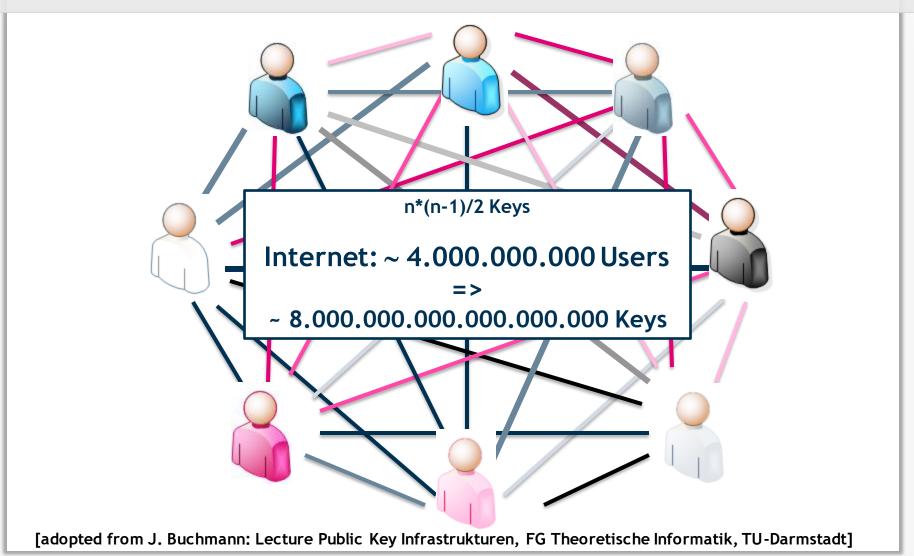
Algorithm	Performance*
RC6	78 ms
SERPENT	95 ms
IDEA	170 ms
MARS	80 ms
TWOFISH	100 ms
DES-ede	250 ms
RIJNDEAL (AES)	65 ms

^{*} Encryption of 1 MB on a Pentium 2.8 GHz, using the FlexiProvider Java)

[J. Buchmann: Lecture Public Key Infrastrukturen, FG Theoretische Informatik, TU-Darmstadt]

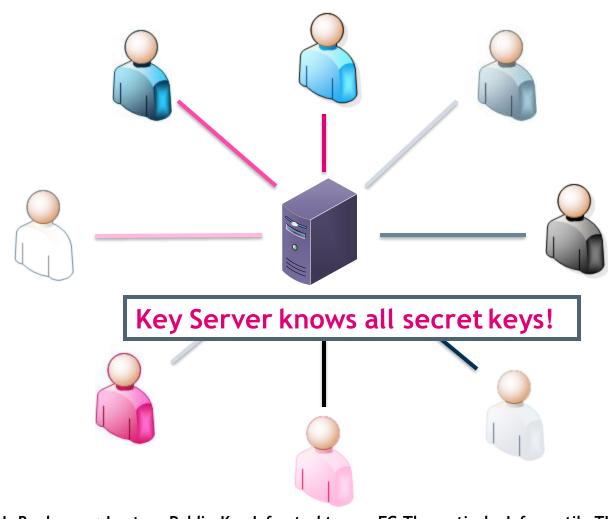


Disadvantage: Key Exchange





A Possible Solution



[J. Buchmann: Lecture Public Key Infrastrukturen, FG Theoretische Informatik, TU-Darmstadt]



Key Management in Symmetric Encoding Systems

Key Distribution Center KDC

- One key per communication pair is necessary.
- Secure agreement and transfer are also challenging.
- A center for key distribution is possible but this party then knows all secret keys!

Secret key, encrypted for A k

Participant A encrypted text

Secret key, encrypted for B

Participant B



Remark

Roger Needham / Butler Lampson

"Anybody who asserts that a problem is readily solved by encryption, understands neither encryption nor the problem."



[Marshall Symposium 1998] [Randell 2004]



References

- [Knospe2019] Knospe, Heiko. A Course in Cryptography. Vol. 40. American Mathematical Soc., 2019. p. 35.
- [Bi2005] Matt Bishop: Introduction to Computer Security. Boston: Addison Wesley, 2005. pp. 97-113
- [The Marshall Symposium] The Marshall Symposium: Address Roger Needham, May 29, 1998, Rackham School of Graduate Studies, University of Michigan web.archive.org/web/20081201182254/http:/www.si.umich.edu/marshall/docs/p201.htm, accessed 2015-04-15.
- [Randell 2004] Randell, B. (2004) *Brief Encounters*; Pp. 229-235 in: Andrew Herbert, Karen Spärck Jones: Computer Systems: Theory, Technology, and Applications; New York, Springer 2004
- [Federrath Pfitzmann 1997] Hannes Federrath, Andreas Pfitzmann: Bausteine zur Realisierung mehrseitiger Sicherheit. in: Günter Müller, Andreas Pfitzmann (Hrsg.): Mehrseitige Sicherheit in der Kommunikationstechnik, Addison-Wesley-Longman 1997, 83-104.